

GCSE MATHEMATICS

Higher tier

Algebra

Topic test – Sequences

v1.0

Name _____

Materials

For this paper you must have:

- Mathematical instruments
- A calculator.



Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 26.

Advice

- In all calculations, show clearly how you work out your answer.

| For Teacher's Use | |
|-------------------|------|
| Pages | Mark |
| 2 - 3 | |
| 4 - 5 | |
| 6 | |
| TOTAL | |

- 1** Here is a linear sequence.
The first two terms are missing.

... ... 5 11 17 23 29 ...

- 1 (a)** Describe how the sequence is building up.

[1 mark]

- 1 (b)** What is the first term of the sequence?

[1 mark]

Answer _____

- 2** The n th term of a sequence is $3n - 1$

- 2 (a)** Work out the first three terms of the sequence.

[1 mark]

Answer _____ , _____ , _____

- 2 (b)** Which term of the sequence has a value of 101?

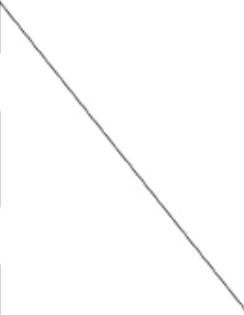
[2 marks]

Answer _____

- 3 Match each sequence to its description.
One has been done for you.

[4 marks]

| | |
|-------------------|------------------------|
| 1 1 2 3 5 8 | Arithmetic progression |
| 1 2 4 8 16 32 | Geometric progression |
| 1 2 3 4 5 6 | Fibonacci sequence |
| 1 3 6 10 15 21 | Triangular numbers |
| 1 4 9 16 25 36 | Cube numbers |
| 1 8 27 64 125 216 | Square numbers |



- 4 All the terms of a **geometric** progression are positive.
The second and fourth terms are shown.

... 9 ... 81

Work out the first and third terms.

[2 marks]

First term _____

Third term _____

5 The n th term of sequence A is $2n + 3$

The n th term of sequence B is $5n - 4$

Work out **two** different terms that are in both sequences.

[2 marks]

Answer _____

6 The n th term of sequence P is $an + b$

The n th term of sequence Q is $bn + a$

6 (a) Show that the sequences both start with the same term.

[1 mark]

6 (b) The 2nd term of sequence P equals the 3rd term of sequence Q .

Show that $a = 2b$

[2 marks]

- 7 A linear sequence starts:

$$a + 6b \quad a + 8b \quad a + 10b \quad \dots\dots \quad \dots\dots$$

The 2nd term has value 46

The 5th term has value 82

Work out the values of a and b .

[4 marks]

$$a = \underline{\hspace{4cm}}$$

$$b = \underline{\hspace{4cm}}$$

- 8 The n th term of a sequence is $\frac{n(n-4)}{\sqrt{n+3}}$

Work out the sum of the second and third terms.

Write your answer in the form $\frac{a\sqrt{5} + b\sqrt{6}}{c}$ for integers a , b and c

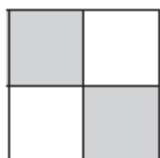
[3 marks]

Answer $\underline{\hspace{4cm}}$

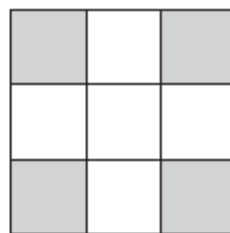
9

A square pattern is made from shaded and plain tiles.

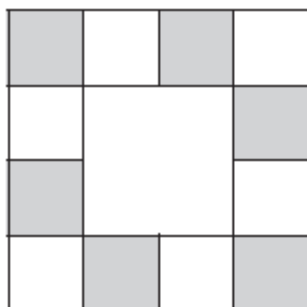
Jon counts how many shaded tiles are in each square pattern.



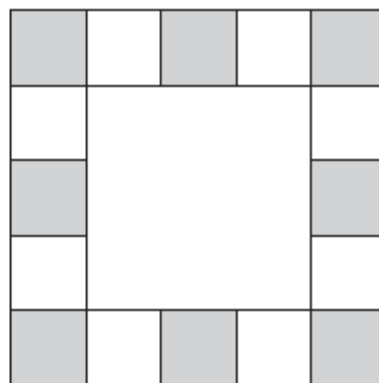
2 shaded tiles



4 shaded tiles



6 shaded tiles



8 shaded tiles

Jon counts 250 shaded tiles around the edges of a square pattern.

How many tiles are along one side of the square?

[3 marks]

Answer _____

END OF QUESTIONS