

Please write clearly in block capitals.

Surname \_\_\_\_\_

Forename(s) \_\_\_\_\_

Candidate signature \_\_\_\_\_

I declare this is my own work.

# GCSE MATHEMATICS

# H

Higher Tier

Paper 3 Calculator

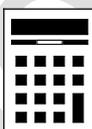
Shadow paper based on June 2022 question paper

Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

## Advice

In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26–27	
<b>TOTAL</b>	

Answer **all** questions in the spaces provided.

Do not write  
outside the  
box

**1** Circle the largest number.

**[1 mark]**

6.78

6. $\dot{7}$

6.708

6.77

**2** Work out  $\begin{pmatrix} 4 \\ -3 \end{pmatrix} - \begin{pmatrix} 6 \\ -8 \end{pmatrix}$

Circle your answer.

**[1 mark]**

$\begin{pmatrix} -2 \\ -5 \end{pmatrix}$

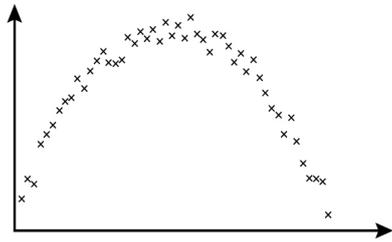
$\begin{pmatrix} 2 \\ -11 \end{pmatrix}$

$\begin{pmatrix} -2 \\ 5 \end{pmatrix}$

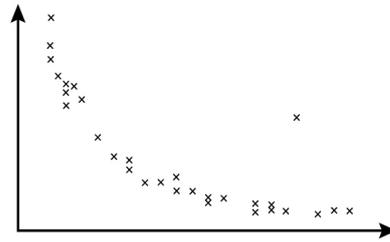
$\begin{pmatrix} -2 \\ -11 \end{pmatrix}$

3 Here are four scatter graphs.

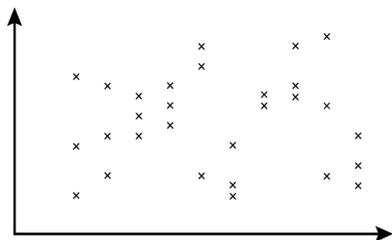
Graph A



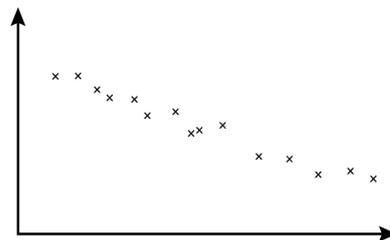
Graph B



Graph C



Graph D



3 (a) Which graph has **one** outlier?  
Circle your answer.

[1 mark]

A

B

C

D

3 (b) For which graph is a straight line of best fit appropriate?  
Circle your answer.

[1 mark]

A

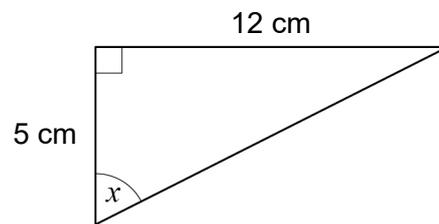
B

C

D

- 4 Use trigonometry to work out the size of angle  $x$ .

Not drawn  
accurately



[3 marks]

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$x =$  \_\_\_\_\_ °

Turn over for the next question

5

Lisa works two days part-time in a shop each month.

The table shows the number of hours she works on Monday and Tuesday in May and June.

	Monday	Tuesday
May	2	3
June	$4\frac{1}{4}$	$3\frac{3}{4}$

Work out the percentage increase in her **total** hours from May to June.

[3 marks]

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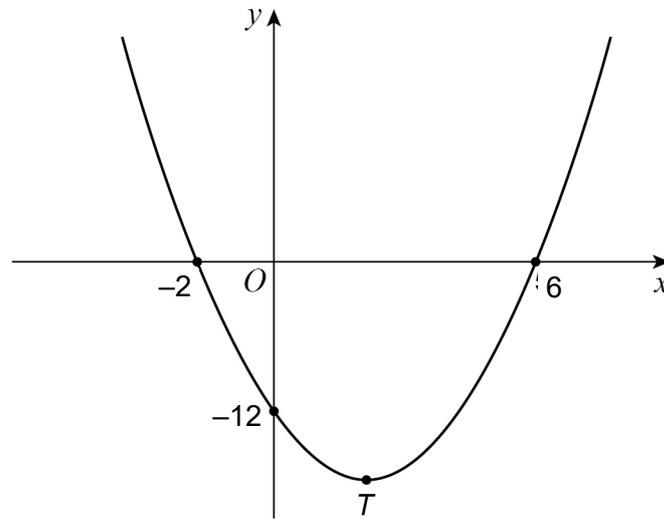
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Answer \_\_\_\_\_ %

Turn over ►

6 Here is a sketch of the curve  $y = x^2 - 4x - 12$



6 (a) Write down the **two** roots of  $x^2 - 4x - 12 = 0$

[1 mark]

Answer \_\_\_\_\_ and \_\_\_\_\_

6 (b) Work out the coordinates of  $T$ , the turning point of the curve.

[2 marks]

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Answer ( \_\_\_\_\_ , \_\_\_\_\_ )

7

A is an **arithmetic** progression.

Here are the first four terms.

11            14            17            20

G is a **geometric** progression.

Here are the first four terms.

4            8            16            32

 $n$ th term of A = 8th term of GWork out the value of  $n$ .**[4 marks]**

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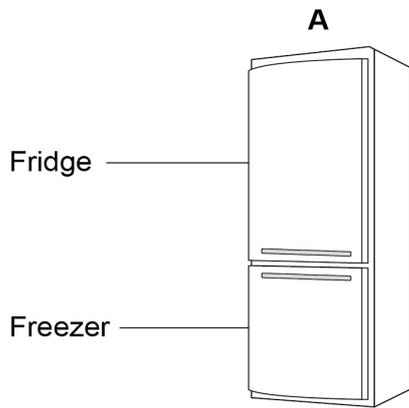
 $n =$  \_\_\_\_\_

7
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**Turn over ►**

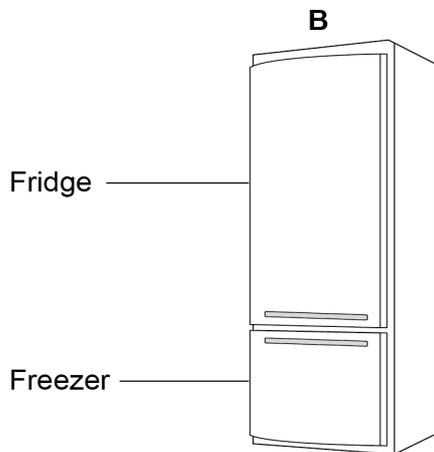
8

Information about two fridge-freezers, A and B, is shown.



**Total** capacity is 380 litres

fridge capacity : freezer capacity = 3 : 2



**Freezer** capacity is 99 litres

fridge capacity : freezer capacity = 7 : 3



9 Tracey and Anita are the two runners in a 400-metre race.

Tracey completes the race in 52 seconds.

Anita completes the race at an average speed of 28.8 kilometres per hour.

Who wins the race?

You **must** show your working.

[3 marks]

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Answer \_\_\_\_\_

**10** The mass of a baby elephant is 120.4 kilograms to 1 decimal place.

What is the error interval for the mass in kilograms?

Tick **one** box.

[1 mark]

$$120.3 \leq \text{mass} \leq 120.5$$

$$120.35 \leq \text{mass} \leq 120.45$$

$$120.3 \leq \text{mass} < 120.5$$

$$120.35 \leq \text{mass} < 120.45$$

**11** A quadrilateral has angles  $70^\circ$ ,  $90^\circ$ ,  $100^\circ$  and  $100^\circ$

Circle the possible type of quadrilateral.

[1 mark]

kite

parallelogram

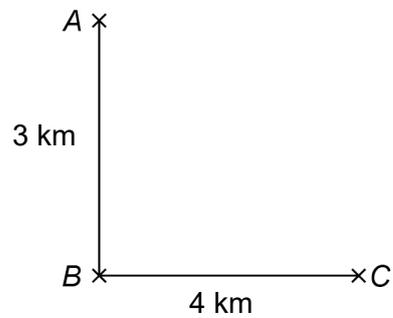
rhombus

trapezium

**Turn over for the next question**

12 (a) B is

3 km due South of A  
and  
4 km due West of C.



Not drawn  
accurately

Work out the bearing of A from C.

[2 marks]

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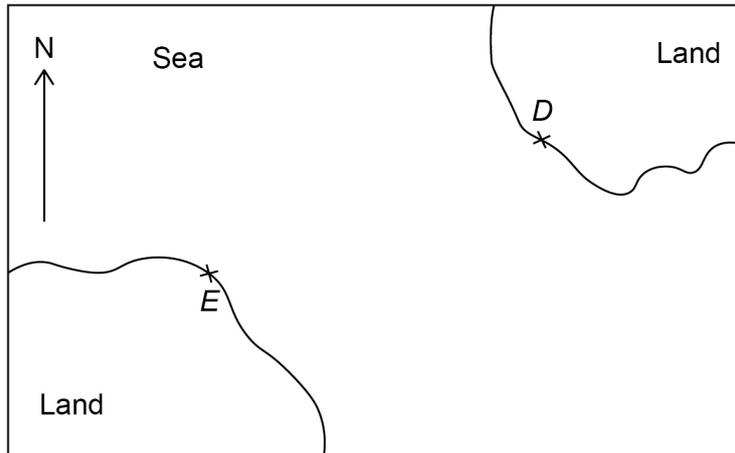
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Answer \_\_\_\_\_ °

12 (b) Here is a scale drawing.



A ship is going to sail from  $E$  to  $D$ .

Molly works out that the ship needs to sail on a bearing of  $248^\circ$

Why must Molly be wrong?

[1 mark]

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13 Simplify  $\sqrt{7a} + \sqrt{7a}$

Circle your answer.

[1 mark]

$7a$

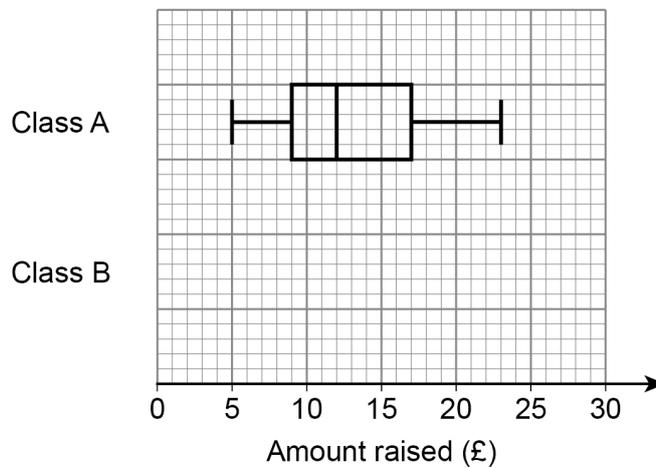
$49a^2$

$2\sqrt{7}a$

$2\sqrt{7a}$

Turn over ►

- 14** People in two villages, A and B, raised money for charity.  
The box plot for class A is shown on the grid.



For class B,

- the lowest amount was £5 and the highest amount was £29
- the lower quartile was £8
- the median was £4 greater than the class A median
- the interquartile range was double the class A interquartile range.

Draw the box plot for village B on the grid.

**[4 marks]**

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15

A town has

a population density of 294 people per km<sup>2</sup>

and

a population of 141 120

$$\text{population density} = \frac{\text{population}}{\text{area}}$$

The population increases to 151 680

Work out the population density after the increase.

**[3 marks]**

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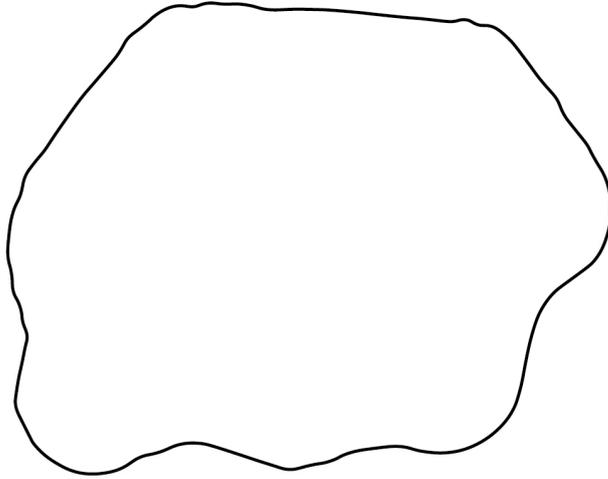
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Answer \_\_\_\_\_ people per km<sup>2</sup>**Turn over ►**

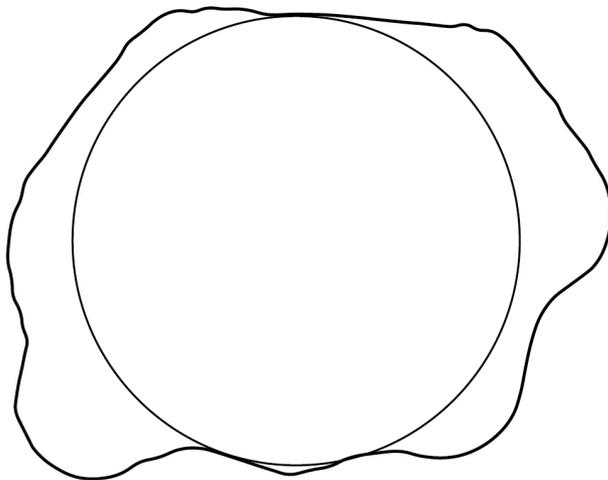
16 Here is a scale drawing of a reservoir.

**Scale:** 1 cm represents 600 m



Vanessa wants to estimate the volume of water in the reservoir.

She draws on the scale drawing a circle with radius 3 cm



- 16 (a)** Vanessa estimates the volume of the reservoir by assuming that
- the reservoir is a cylinder whose cross section is the circle
  - the depth of the reservoir is 19 metres.

Work out Vanessa's estimate in cubic metres.

**[3 marks]**

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Answer \_\_\_\_\_ m<sup>3</sup>

- 16 (b)** In fact,
- the depth of the reservoir is 15 metres
  - the reservoir is **not** a cylinder (see diagram).

Which statement about the actual volume of the reservoir is correct?

Tick **one** box.

It is less than Vanessa's estimate

It is greater than Vanessa's estimate

It could be less than or greater than Vanessa's estimate

Give a reason for your answer.

**[2 marks]**

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5

**Turn over ►**

- 17** In a restaurant, diners can choose their meal combinations.  
They choose one of each from
- 5 starters
  - 10 main dishes
  - 8 desserts

- 17 (a)** How many different meal combinations can be made?

**[2 marks]**

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Answer \_\_\_\_\_

- 17 (b)** Two meal combinations are chosen at random.  
What is the probability that they are exactly the same?

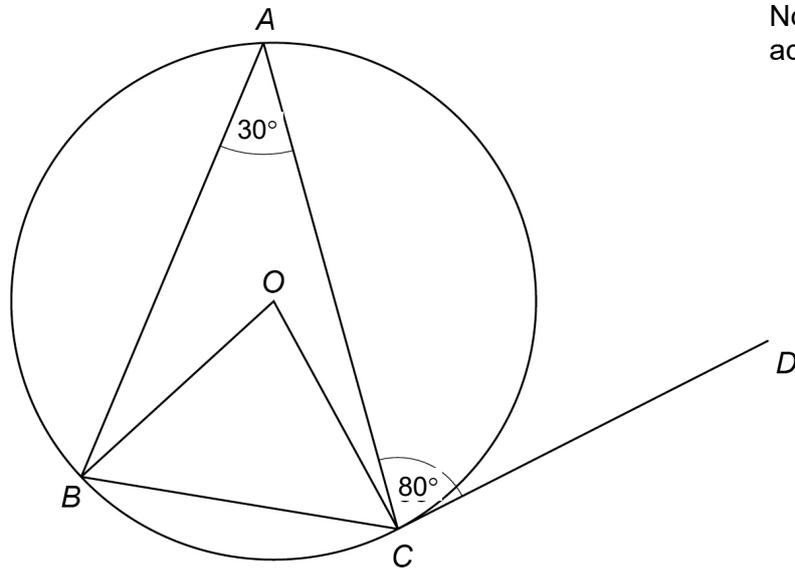
**[1 mark]**

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Answer \_\_\_\_\_

- 18  $A$ ,  $B$  and  $C$  are points on a circle, centre  $O$ .  
 $DC$  is a tangent to the circle.



Show that  $\text{angle } ACO : \text{angle } ABO = 1 : 2$

[5 marks]

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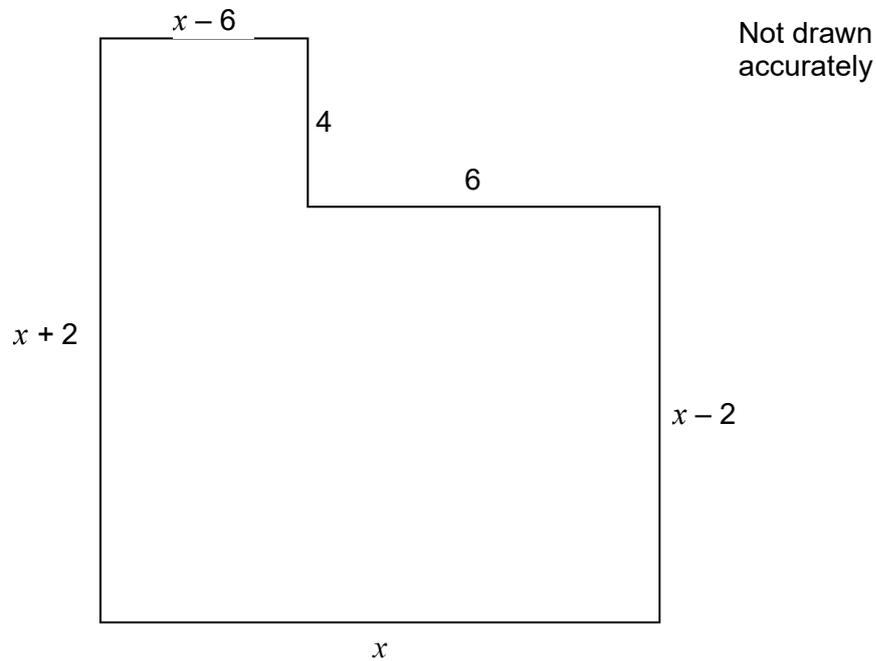
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Turn over ►

- 19** Here is the plan of the floor of an L-shaped room.  
All lengths are in metres.



- 19 (a)** The area of the floor is  $119\text{m}^2$

Show that  $x^2 + 2x - 143 = 0$

**[3 marks]**

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**19 (b)** By factorising  $x^2 + 2x - 143$  work out the value of  $x$ .

You **must** show your working

**[2 marks]**

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$x =$  \_\_\_\_\_

**20** £2448 is invested in an account at a rate of compound interest.  
One year after the investment there is £2509.20 in the account.

How much is in the account five years after the investment?

**[3 marks]**

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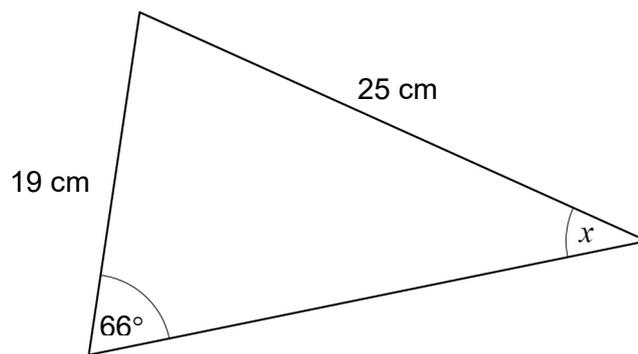
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Answer £ \_\_\_\_\_

**Turn over ►**

21

Not drawn  
accuratelyUse the sine rule to work out the size of angle  $x$ .**[3 marks]**

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$$x = \underline{\hspace{10em}}^\circ$$

22

$$f(x) = 3x \quad \text{and} \quad g(x) = x^2$$

Circle the expression for  $gf(x)$ **[1 mark]**

$3x^2$

$9x^2$

$3x^3$

$9x^4$

23

Here are two simultaneous equations.

$$y = x^2 + 5x + a$$

and

$$y = 4x - b$$

There is a solution when  $x = 6$ Work out the value of  $a + b$ **[3 marks]**

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Answer \_\_\_\_\_

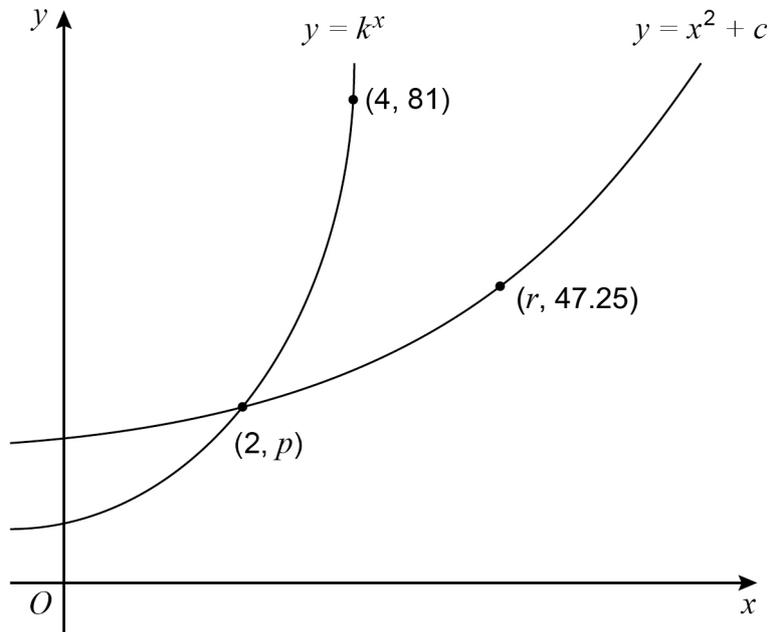
**Turn over for the next question**

7
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**Turn over ►**

24

Here is a sketch of the graphs of  $y = k^x$  and  $y = x^2 + c$   
 $k$  and  $c$  are positive constants.



Work out the value of  $r$ .

[4 marks]

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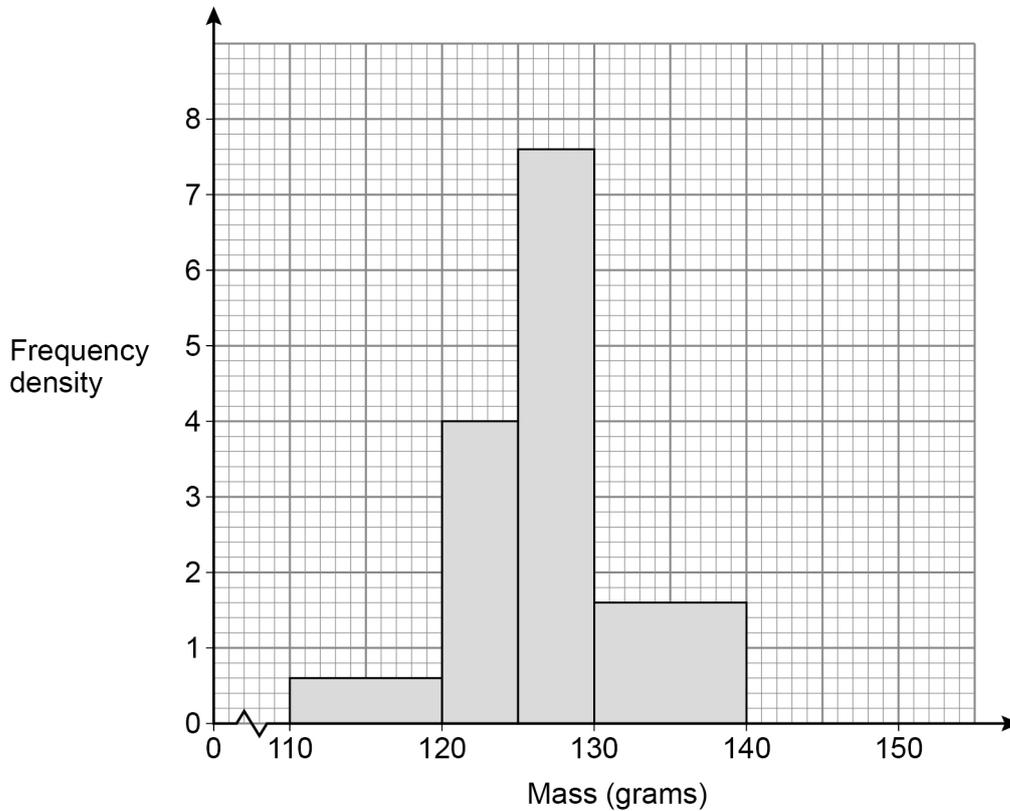
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$r =$  \_\_\_\_\_

**25** A company makes light bulbs.  
The masses of 80 light bulbs are checked.  
A histogram is drawn to represent the data.



The company makes 42 000 light bulbs each day.

Estimate how many light bulbs made each day have a mass **greater than** 124 grams.

**[4 marks]**

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Answer \_\_\_\_\_

**Turn over ►**

**26**  $Q$  and  $R$  are two numbers.

As a product of prime factors,

$$Q = 3^3 \times 5 \times a^3$$

$$R = 3^4 \times 5^2 \times a^2$$

**26 (a)** The highest common factor (HCF) of  $Q$  and  $R$  is 6615

Work out the value of  $a$ .

**[2 marks]**

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$$a = \underline{\hspace{10cm}}$$

**26 (b)** Work out the lowest common multiple (LCM) of  $Q$  and  $R$ .

**[2 marks]**

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$$\text{Answer } \underline{\hspace{10cm}}$$



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