AQA

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

GCSE MATHEMATICS

H

Higher Tier

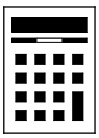
Paper 3 Calculator

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice

In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26–27	
28–29	
TOTAL	

Answer **all** questions in the spaces provided.

Do not write outside the box

1 $3^x = 81$

Circle the value of x.

[1 mark]

3 4 5 6

2 What is 2.9×10^{-3} as an ordinary number?

Circle your answer.

[1 mark]

$-29\,000$ $-2\,900$ $0.002\,9$ $0.000\,29$

Do not write outside the box

3 Expand $6x^3(x^2 + 2)$

Circle your answer.

[1 mark]

$6x^5 + 2$ $6x^6 + 2$ $6x^5 + 12x^3$ $6x^6 + 12x^3$

4 $30 < x < 300$

x is 150% of y

Circle the correct inequality.

[1 mark]

$15 < y < 150$ $20 < y < 200$ $45 < y < 450$ $90 < y < 900$

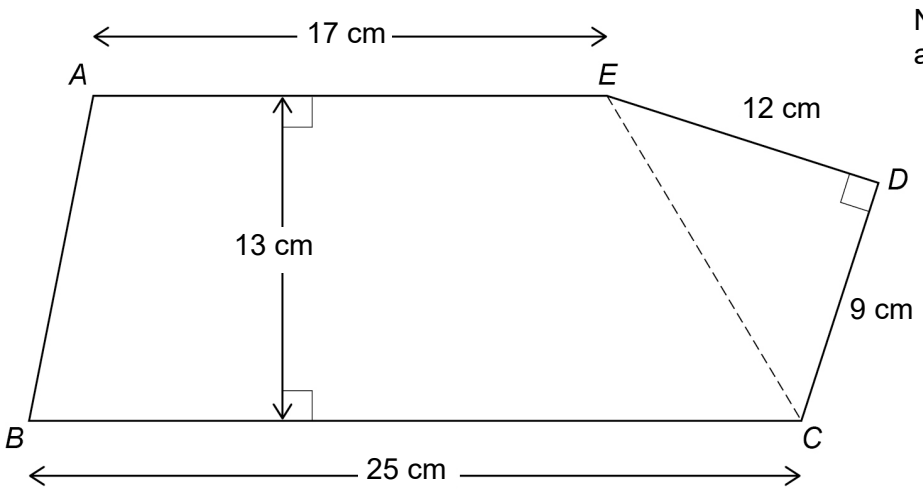
Turn over for the next question

4

Turn over ►

Do not write outside the box

5 *ABCDE* is a pentagon.



Not drawn accurately

Work out the area of the pentagon.

[3 marks]

Answer _____ cm^2

Do not write outside the box

6 Jenny, Kevin and Liqiu each have an amount of money.

Jenny has £96

Jenny's amount : Kevin's amount = 8 : 3

Liqiu's amount is $2\frac{1}{2}$ times Jenny's amount.

Show that, in total, they have **more** than £350

[3 marks]

Turn over for the next question

6

Do not write outside the box

7 (a) Here is the rule for a sequence.

> After the first two terms, each term is the sum of the previous two terms

The 1st term is 26

The 2nd term is x

The 4th term is 84

Work out the value of x.

[3 marks]

$x =$ _____

7 (b) An expression for the nth term of a different sequence is $n^2 - 2n$

Jamie says,

''All the terms will be positive because n^2 is always greater than $2n$.''

Is he correct?

Tick a box.

☐ Yes ☐ No

Give a reason for your answer.

[1 mark]

Do not write outside the box

8 Here is some information about the members of gyms A and B.

	Number of members	**Mean weight of members**
Gym A	56	68 kg
Gym B	32	85 kg

Work out $\dfrac{\text{total weight of the members of gym A}}{\text{total weight of the members of gym B}}$

Give your answer as a decimal.

[2 marks]

Answer _____

Turn over for the next question

6

Do not write outside the box

9 *P* and *Q* are points.

The x-coordinate of *Q* is 5 **less** than the x-coordinate of *P*.

The y-coordinate of *Q* is 8 **more** than the y-coordinate of *P*.

Work out the gradient of the straight line through *P* and *Q*.

[2 marks]

Answer _____

Do not write outside the box

10 Here are the results after 200 spins of a coin.

Heads	104
Tails	96

The coin is spun an extra 20 times.

After all 220 spins, the relative frequency of Heads is 0.55

For the **extra 20 spins**, work out number of Heads : number of Tails

[3 marks]

Answer _____ : _____

Turn over for the next question

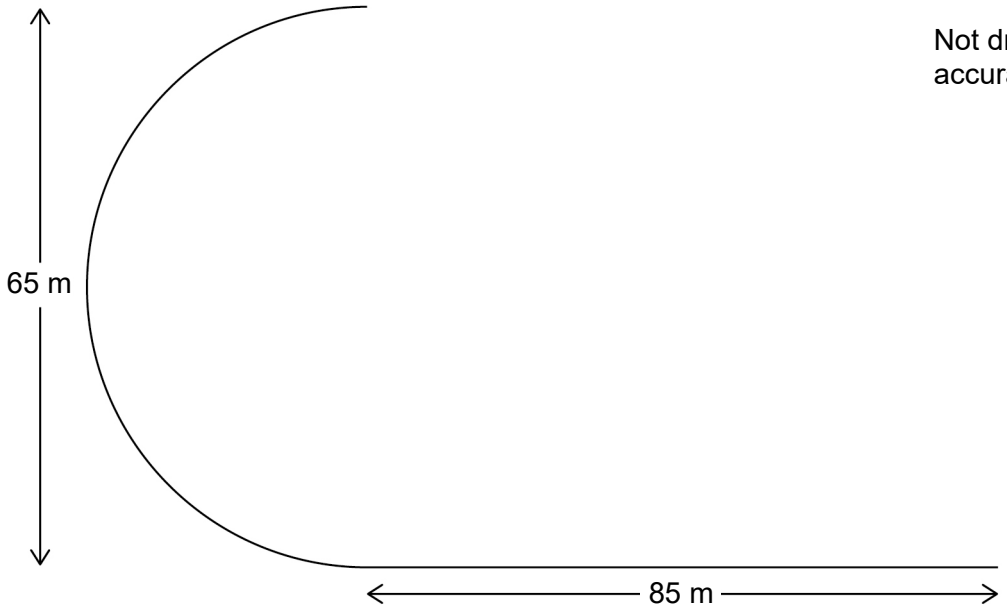
5

Do not write outside the box

11 Part of a running track is the arc of a semicircle joined to a straight line.

The semicircle has diameter 65 metres.

The straight line has length 85 metres.



Not drawn accurately

Alison runs once along this part of the track in 24 seconds.

Work out her average speed.

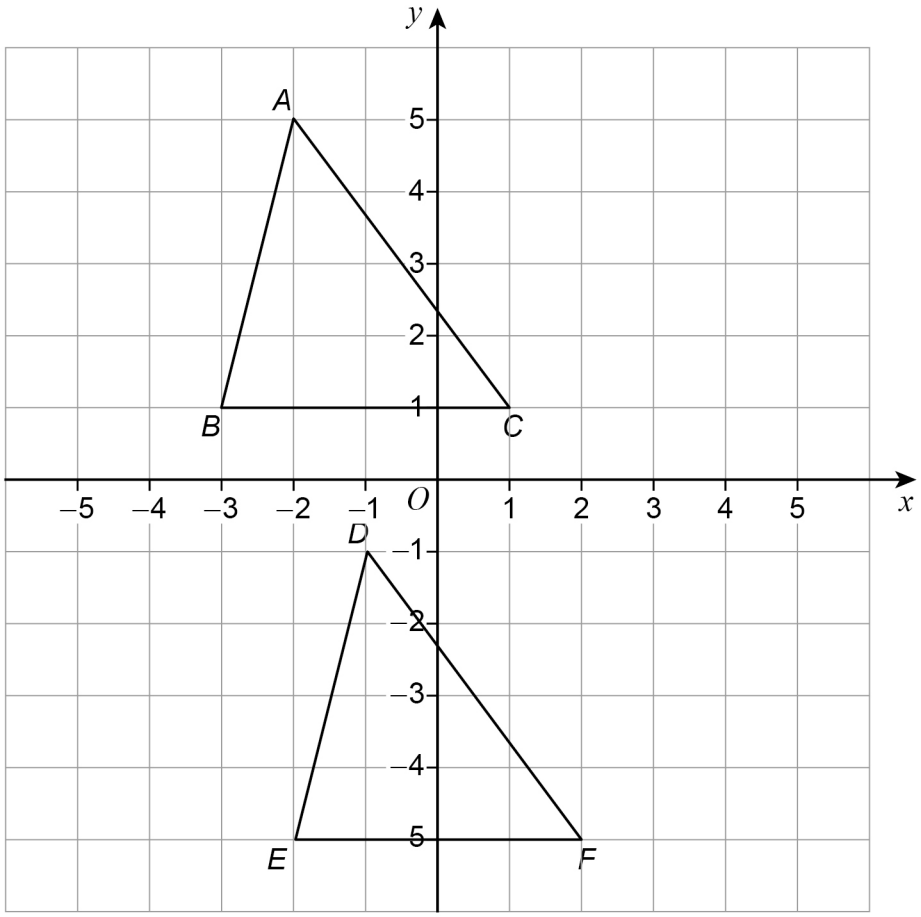
Give your answer to 2 significant figures.

[4 marks]

Answer _____ m/s

Do not write outside the box

12 Triangles *ABC* and *DEF* are shown on a grid.



Describe a single transformation that shows the triangles are congruent.

[2 marks]

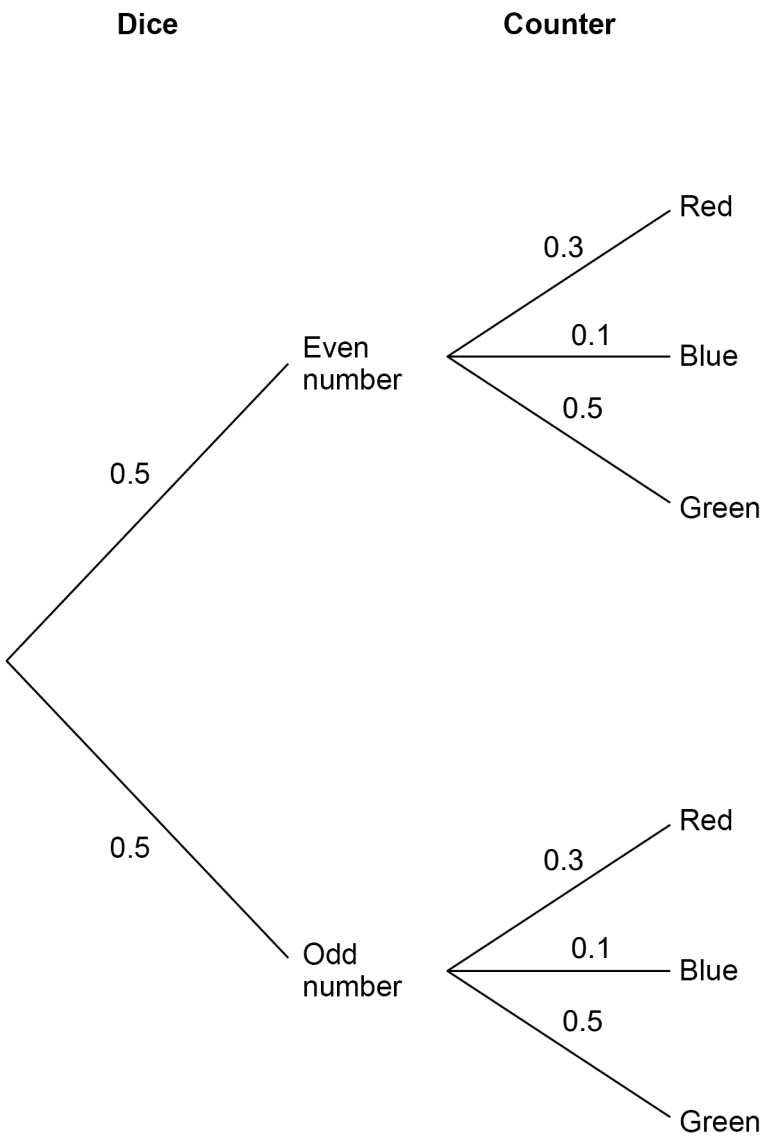
6

Turn over ►

Do not write outside the box

13 A fair, ordinary dice is rolled and a counter is taken at random from a bag.

The tree diagram shows the probabilities.



Do not write outside the box

13 (a) How do the probabilities show that not **all** of the counters in the bag are red, blue or green?

[1 mark]

13 (b) Circle the probability that the counter is red **or** green.

[1 mark]

0.9 0.7 0.8 0.15

13 (c) Circle the probability that the dice lands on an odd number **and** the counter is red.

[1 mark]

0.15 0.3 0.35 0.8

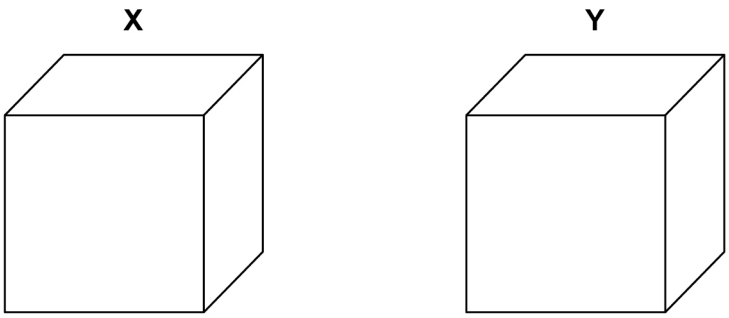
Turn over for the next question

Do not write outside the box

14 Here are two solid cubes, X and Y.

The mass of X is 8.5169 kg

The area of **each face** of X is 529 cm^2



mass 8.5169 kg

14 (a) Zara wants to know the density of Y.

She assumes that Y is identical to X.

What density should she get for Y?

Give your answer in **grams per cubic centimetre**.

[4 marks]

Answer _____ g/cm^3

Do not write outside the box

14 (b) In fact,

the mass of Y is greater than the mass of X

the area of each face of Y is greater than the area of each face of X.

What does this mean about the actual density of Y?

Tick **one** box.

[1 mark]

☐ It is less than the answer to part (a)

☐ It is equal to the answer to part (a)

☐ It is greater than the answer to part (a)

☐ It is not possible to tell

Turn over for the next question

5

Turn over ►

Do not write outside the box

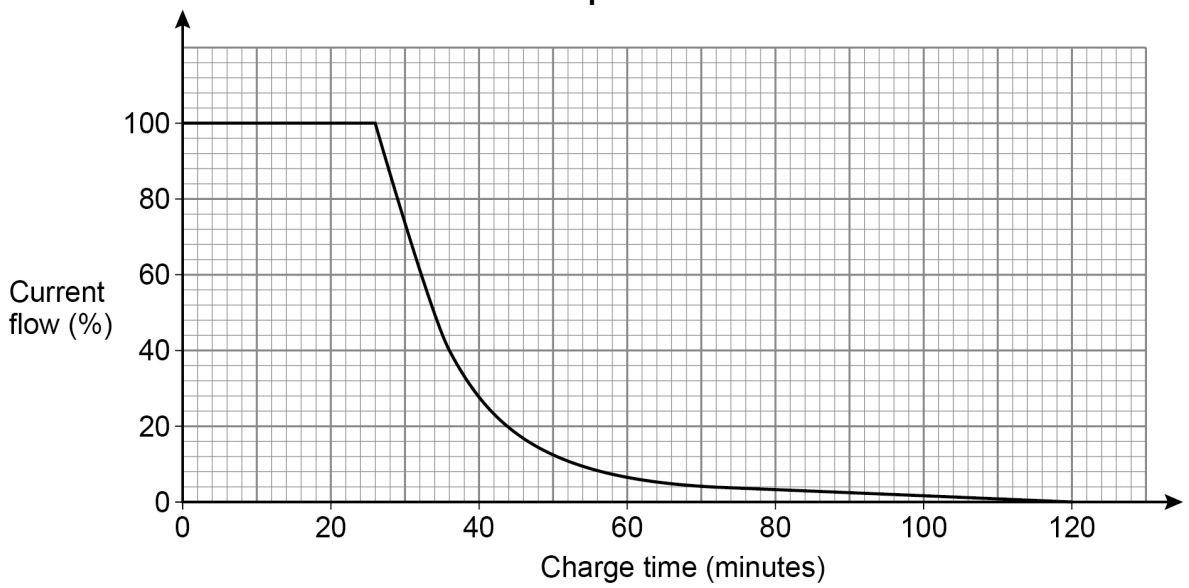
15 A battery takes 2 hours to charge from empty.

When the battery is being charged, the current flow into the battery

- starts at full current flow (100%)
- continues at full current flow for a period of time
- gradually decreases until the battery is fully charged.

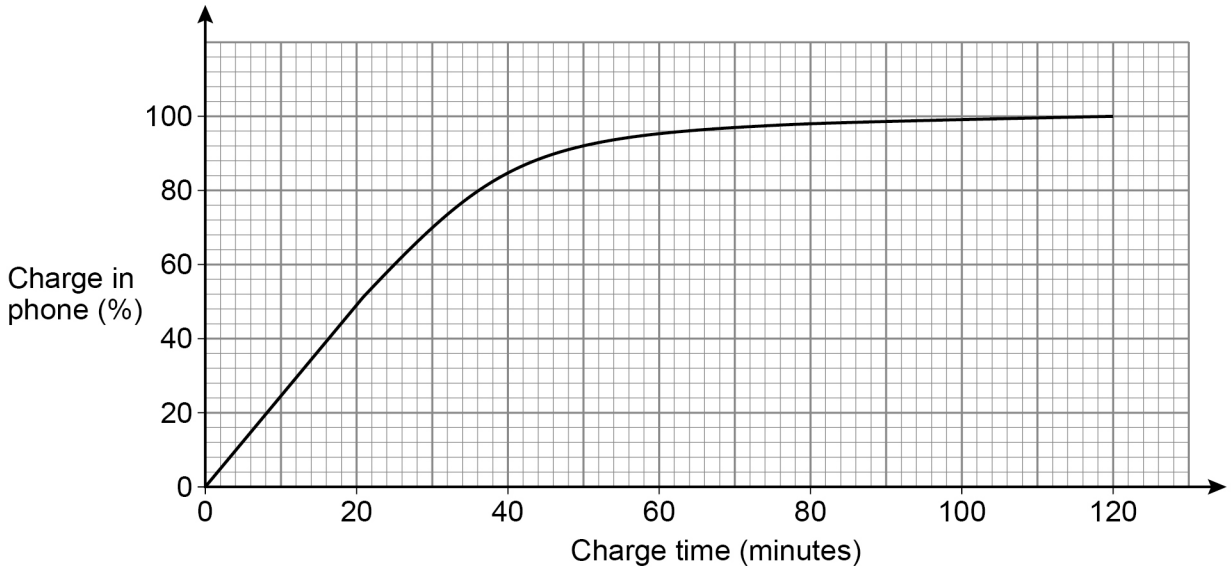
This is shown on **Graph A** below.

Graph A



Graph B shows the percentage charge in the battery when charging from empty.

Graph B



Do not write outside the box

Maureen's battery is empty of charge.

She starts to charge her battery at 9.00 am

15 (a) Using **Graph A**,

estimate the time when the current flow starts to decrease.

[2 marks]

Answer _____ am

15 (b) Using **Graph A and Graph B**,

estimate the percentage charge in the battery when the current flow is 60%

[1 mark]

Answer _____ %

15 (c) Using **Graph B**,

estimate the rate of increase in the percentage charge when the battery has 80% charge.

[2 marks]

Answer _____ percent per minute

5

Turn over ►

Do not write outside the box

16 R is inversely proportional to the square root of S.

$R = 3$ when $S = 49$

16 (a) Work out an equation connecting R and S.

[3 marks]

Answer _____

16 (b) Work out the value of R when $S = 9$

[2 marks]

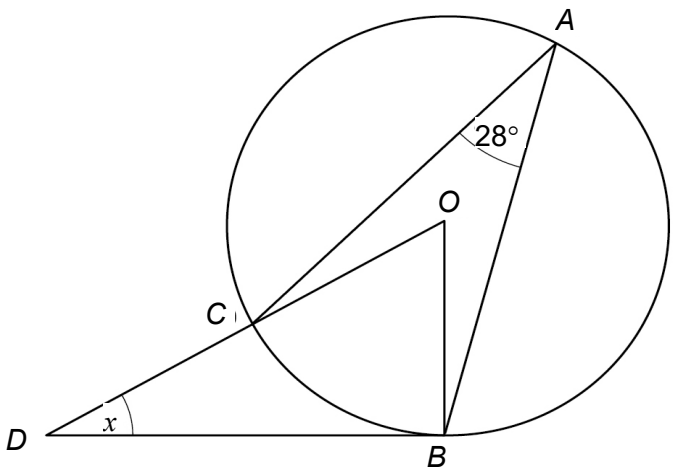
$R =$ _____

Do not write outside the box

17 *A*, *B* and *C* are points on a circle, centre *O*.

BD is a tangent to the circle.

OCD is a straight line.



Not drawn accurately

Work out the size of angle x.

[3 marks]

$x =$ _____ degrees

8

Turn over ►

Do not write outside the box

18 Rearrange $5(3g - 2) + 7g = hg + h^3$ to make g the subject.

[4 marks]

Answer _____

19 A circle has centre (0, 0) and passes through (0, 13)

Write down the equation of the circle.

[1 mark]

Answer _____

Do not write outside the box

20 There should be a bus leaving a bus station every hour from 6 am
No buses leave early.

P(the **first bus** leaves on time) = 0.85

For all the **other buses**,

if the previous bus did leave on time, P(this bus leaves on time) = 0.8

if the previous bus did **not** leave on time, P(this bus leaves on time) = 0.75

20 (a) Work out P(the first three buses leave on time)

[2 marks]

Answer _____

20 (b) The 2 pm bus does **not** leave on time.

Work out P(exactly one of the next two buses does **not** leave on time)

[3 marks]

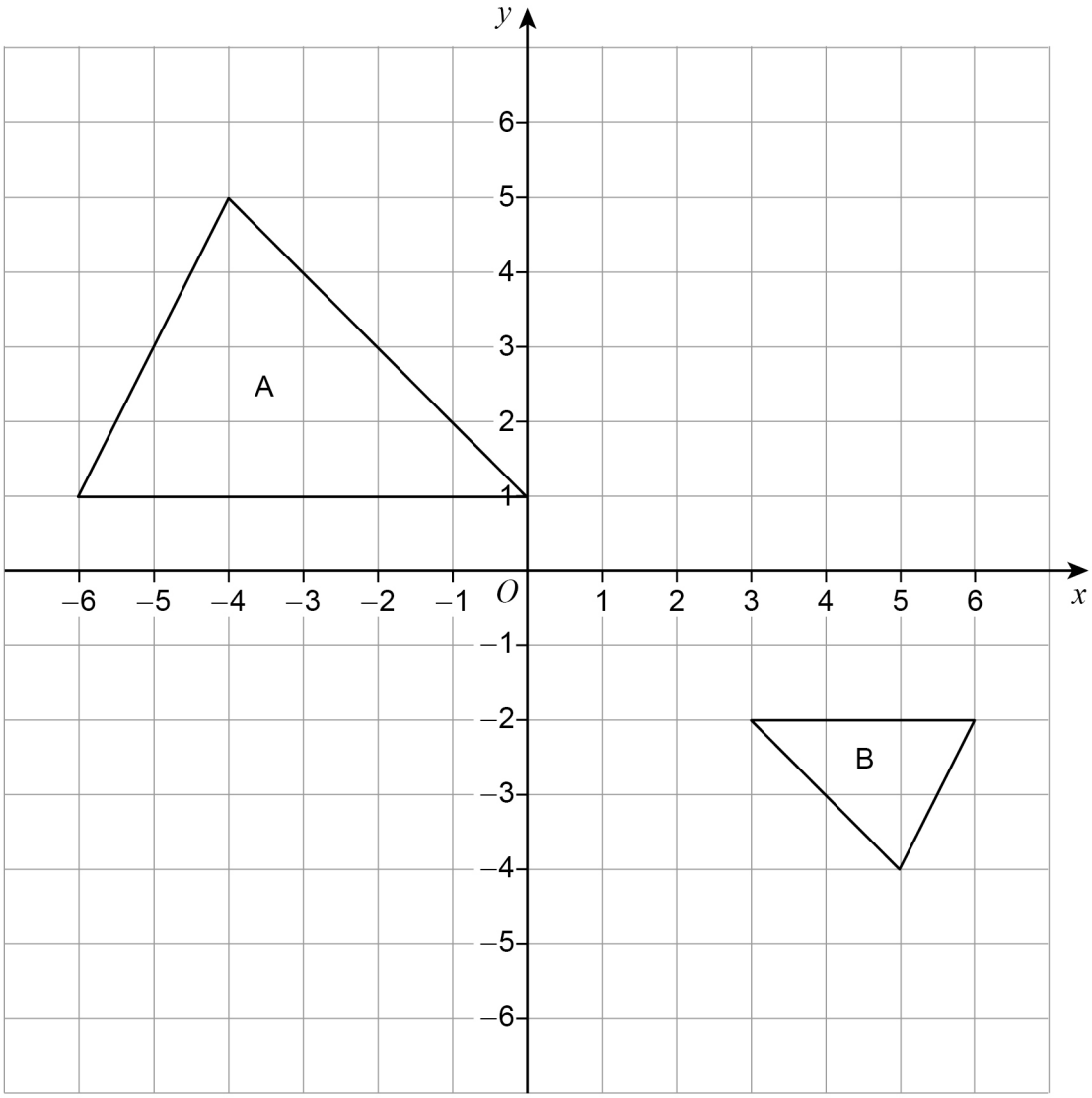
Answer _____

10

Turn over ►

Do not write outside the box

21 Shape B is enlarged to shape A.



21 (a) Circle the scale factor of the enlargement.

[1 mark]

$-\frac{1}{2}$ -2 $\frac{1}{2}$ 2

21 (b) Write down the coordinates of the centre of enlargement.

[1 mark]

Answer (_____ , _____)

Do not write outside the box

22 Simplify fully $\frac{3}{x+2} + \frac{5x-6}{2} + 3x$

Give your answer as a single fraction.

[4 marks]

Answer _____

6

Turn over ►

Do not write outside the box

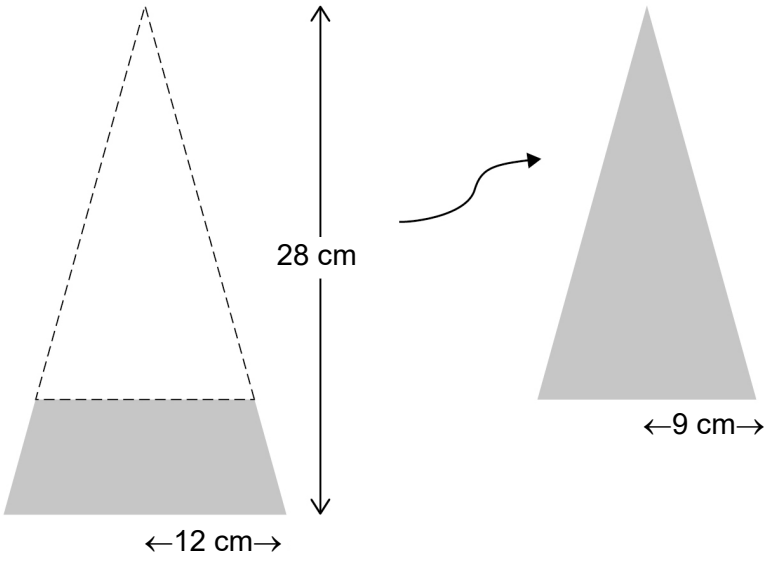
23 Aaron makes a bowl for cat food from a solid wooden cone.

The sketches show how the bowl is made.

The cone has radius 12 cm and perpendicular height 28 cm

A smaller cone, with radius 9 cm, is removed.

Not drawn accurately

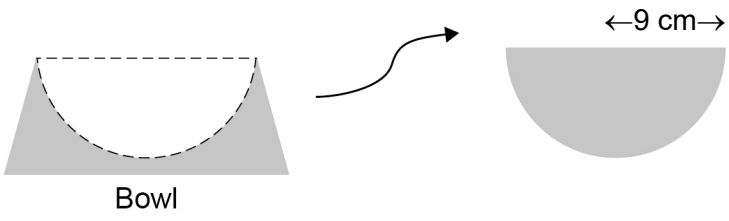


Volume of a cone $= \frac{1}{3}\pi r^2 h$

where r is the radius and h is the perpendicular height

A hemisphere with radius 8 cm is then removed.

Not drawn accurately



Volume of a hemisphere $= \frac{2}{3}\pi r^3$ where r is the radius

Do not write outside the box

Work out the volume of the remaining wood that forms the bowl.

[5 marks]

Answer _____ cm^3

5

Do not write outside the box

24 On the same day, an investor buys

a boat for £150 000

and

a house for £120 000

The value of the boat decreases by 25% in the first year, and then by 10% each year.

The value of the flat increases by 5% each year.

Show that the flat becomes worth two times more than the boat during the fifth year.

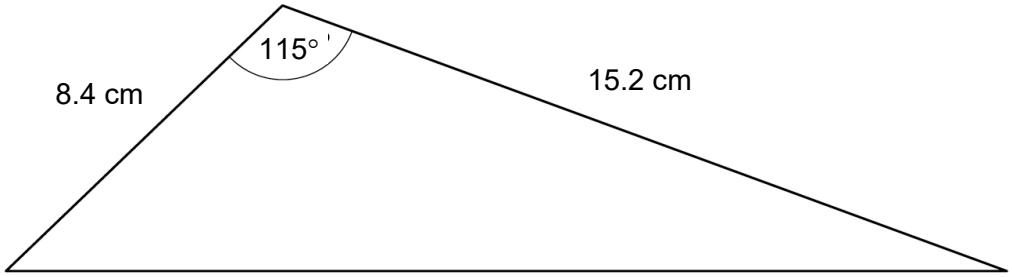
[5 marks]

Do not write outside the box

25 Two sides of a triangle are measured to 1 decimal place.

The angle between the sides is measured to the nearest degree.

Not drawn accurately



Work out the lower bound for the area of the triangle.

You **must** show your working.

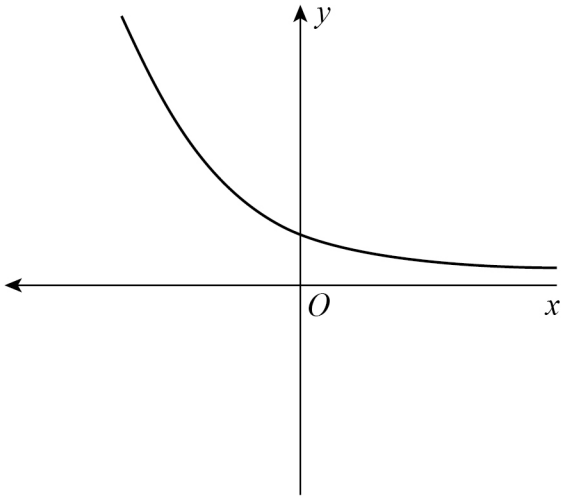
[4 marks]

Answer _____ cm^2

Turn over for the next question

Do not write outside the box

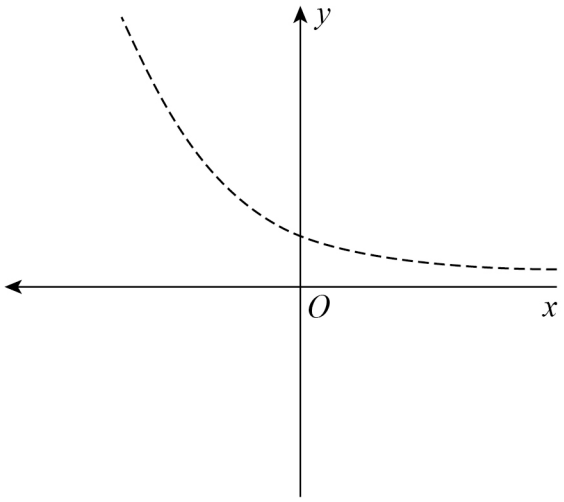
26 Here is a sketch of the graph of $y = 3^{-x}$



In parts (a) and (b) the sketch of $y = 3^{-x}$ is shown as a dashed line.

26 (a) On the axes below, sketch the graph of $y = -3^{-x}$

[1 mark]

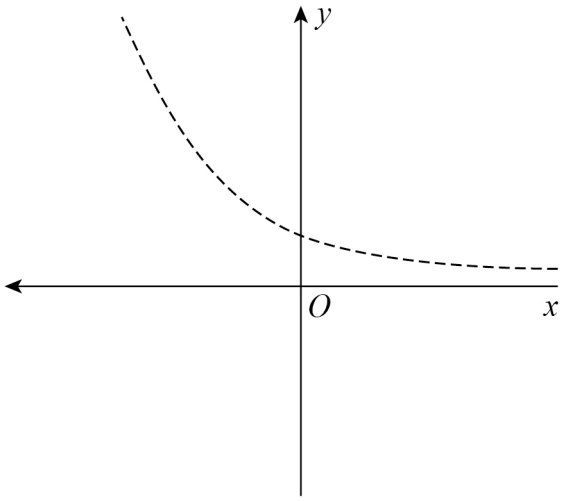


9

Do not write outside the box

26 (b) On the axes below, sketch the graph of $y = 3^{-x} - 2$

[1 mark]



END OF QUESTIONS

2

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